

Study of the decay $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ and observation of an isovector partner to $f_0(1710)$

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Using e^+e^- annihilation data corresponding to a total integrated luminosity of 6.32 fb^{-1} collected at center-of-mass energies between 4.178 and 4.226 GeV with the BESIII detector, we perform an amplitude analysis of the decay $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ for the first time. An enhancement is observed in the $K_S^0 K_S^0$ mass spectrum near $1.7 \text{ GeV}/c^2$, which was not seen in $D_s^+ \rightarrow K^+ K^- \pi^+$ in an earlier work, implying the existence of an isospin one partner of the $f_0(1710)$. The branching fraction of the decay $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ is determined to be $\mathcal{B}(D_s^+ \rightarrow K_S^0 K_S^0 \pi^+) = (0.68 \pm 0.04_{\text{stat}} \pm 0.01_{\text{syst}})\%$.

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The constituent quark model has been successful in explaining the composition of hadrons in the past few decades. In this model, many of the observed light mesons can be described as $q\bar{q}$ states grouped into SU(3) flavor multiplets. In some recent works [1–3], the $f_0(500)$ and $f_0(980)$ mesons are considered to be the ground state SU(3) singlet and octet scalar isoscalar mesons, and the $a_0(980)$ meson is their isovector partner. The SU(3) singlet $f_0(1370)$ and octet $f_0(1500)$ are then considered to be the radial excited states of the $f_0(500)$ and $f_0(980)$ mesons, respectively, with an isovector partner in the $a_0(1450)$. However, in case of the next radial excitation in [2,3], for the singlet $f_0(1710)$ and the newly-identified octet state $f_0(1770)$, no corresponding isovector $a_0(1710)$ meson has been established yet.

On the other side, although the $f_0(1710)$ is well established in the PDG [4], its quark structure is still unclear. The two most possible candidates are a glueball or a vector-vector, i.e., $K^* \bar{K}^*$, molecule [1,5,6]. If the $f_0(1710)$ is a $K^* \bar{K}^*$ molecule, there should be an isovector partner $a_0(1710)$, just as the nearly degenerate $f_0(980)$ and $a_0(980)$ for the case of $K\bar{K}$ molecules. If it is a glueball, a second state as pure glueballs must be isoscalar. Therefore, whether $a_0(1710)$ exists is crucial to understand the picture of $f_0(1710)$.

The BABAR collaboration recently claimed the observation of a new $a_0(1710)^\pm$ resonance in the decay to $\pi^\pm \eta$ with a mass of approximately $1.7 \text{ GeV}/c^2$ in the $\eta_c \rightarrow \eta \pi^+ \pi^-$ decay on the $\eta \pi^\pm$ spectrum [7], but no study for $a_0(1710)$ on the $K\bar{K}$ spectrum yet due to the expected heavy interference between $a_0(1710)^0$ and $f_0(1710)$. Constructing isospin eigenstates from kaon pairs, we obtain $(|K^+ K^- \rangle - |K^0 \bar{K}^0 \rangle)$ for isospin one, while $(|K^+ K^- \rangle + |K^0 \bar{K}^0 \rangle)$ for isospin zero. It follows that if the interference between an f_0 and an a_0 is constructive in decays to a $K^+ K^-$ pair, it is destructive in decays to a pair of neutral kaons and vice versa. A comparison between decays involving $K^+ K^-$ and $K_S^0 K_S^0$

pairs can thus give access to such interference terms and allows a search for the $a_0(1710)^0$ in decays to two kaons.

Furthermore, analyses of D_s decays are an important input for studies of the B_s^0 meson, which predominantly decays to $D_s + X$ [4]. In addition, hadronic D_s decays probe the interplay of short-distance weak-decay matrix elements and long-distance QCD interactions. The measurement of BFs of hadronic D_s decays provides valuable information to help understand strong force-induced amplitudes and phases [8–12].

The BESIII and the BABAR collaborations reported analyses of the $D_s^+ \rightarrow K^+ K^- \pi^+$ decay [13,14] and observed contributions of the scalar mesons $S(980)$ [where $S(980)$ denotes an admixture of $a_0(980)^0$ and $f_0(980)$] and $f_0(1710)$, which is helpful to understand the properties of $f_0(980)$ and $a_0(980)^0$ [15,16]. Both collaborations reported consistent results for the branching fractions (BF) $\mathcal{B}(D_s^+ \rightarrow S(980) \pi^+, S(980) \rightarrow K^+ K^-) = (1.05 \pm 0.04_{\text{stat}} \pm 0.06_{\text{syst}})\%$ and $\mathcal{B}(D_s^+ \rightarrow f_0(1710) \pi^+, f_0(1710) \rightarrow K^+ K^-) = (0.10 \pm 0.02_{\text{stat}} \pm 0.03_{\text{syst}})\%$ [13]. The CLEO collaboration measured the absolute BF of the decay $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ to be $(0.77 \pm 0.05_{\text{stat}} \pm 0.03_{\text{syst}})\%$ [17], using a dataset corresponding to a luminosity of 586 pb^{-1} at a center-of-mass energy of 4.17 GeV. In this work, we present the first amplitude analysis and a more precise measurement of the BF of the $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ decay using 6.32 fb^{-1} of data samples collected at center-of-mass energies of 4.178, 4.189, 4.199, 4.209, 4.219 and 4.226 GeV with the BESIII detector. We do not distinguish between the $a_0(1710)^0$ and $f_0(1710)$ [$a_0(980)$ and $f_0(980)$] mesons, and denote the combined state as $S(1710)$ [$S(980)$]. Charge conjugation is implied throughout this paper.

The BESIII detector [18,19] records symmetric e^+e^- collisions provided by the BEPCII storage ring [20]. The cylindrical core of the BESIII detector covers 93% of the full solid angle and consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The end cap TOF system was upgraded in 2015 using multigap resistive plate chamber technology [21].

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Simulated data samples produced with GEANT4-based [22] Monte Carlo (MC) software, which includes the geometric description of the BESIII detector and the detector response, are used to determine detection efficiencies and to estimate backgrounds. The simulation models the beam energy spread and initial state radiation (ISR) in the e^+e^- annihilations with the generator KKMC [23]. The inclusive MC sample includes the production of open charm processes, the ISR production of vector charmonium(-like) states, and the continuum processes incorporated in KKMC [23]. The known decay modes are modeled with EVTGEN [24] using BFs taken from the Particle Data Group [4], and the remaining unknown charmonium decays are modeled with LUNDCHARM [25]. Final state radiation (FSR) from charged final state particles is incorporated using PHOTOS [26].

The process $e^+e^- \rightarrow D_s^{*\pm} D_s^\mp \rightarrow \gamma D_s^+ D_s^-$ allows studies of D_s^+ decays with a tag technique [27]. There are two types of samples used in the tag technique: single tag (ST) and double tag (DT). In the ST sample, a D_s^- meson is reconstructed through a particular hadronic decay without any requirement on the remaining measured tracks and EMC showers. In the DT sample, a D_s^+ , designated as the ‘‘signal,’’ is reconstructed through $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$, while a D_s^- , designated as ‘‘tag,’’ is reconstructed through one of eight hadronic decay modes: $D_s^- \rightarrow K_S^0 K^-$, $K^+ K^- \pi^-$, $K^+ K^- \pi^- \pi^0$, $K_S^0 K^- \pi^- \pi^+$, $K_S^0 K^+ \pi^- \pi^-$, $\pi^- \pi^- \pi^+$, $\pi^- \eta'$, and $K^- \pi^- \pi^+$. A detailed description of selection conditions concerning charged and neutral particle candidates, the mass recoiling against D_s^\pm candidates, and the mass of the tag candidates are provided in Refs. [28–30].

As in Refs. [29,30], an eight-constraint (8C) kinematic fit is performed to select signal events for the amplitude analysis. Besides the constraints arising from four-momentum conservation, the invariant masses of the two K_S^0 candidates, the tag D_s^- , and the $D_s^{*+(-)}$ candidates are constrained to their known values given in Ref. [4]. If there are multiple signal combinations, the candidate with the minimum χ^2 of the 8C kinematic fit is chosen. Signal D_s^+ candidates are selected if their invariant mass is in the interval [1.950, 1.990] GeV/ c^2 . A further kinematic fit including a ninth constraint on the mass of the signal D_s^+ is performed, and the updated four-momenta are used for the amplitude analysis. This ensures that all candidates fall within the phase space boundary. In total, 412 events are selected with a purity of $f_s = (97.3 \pm 0.8)\%$. The purity is determined from a fit to the invariant mass distribution of the signal D_s^+ candidates.

This analysis uses an isobar formulation in the covariant tensor formalism [31]. Each of intermediate processes can be demonstrated by $D_s \rightarrow ar(\rightarrow bc)$, where r denotes intermediate state, a , b and c are final state particles. Coherently summing the amplitudes of all intermediate processes can obtain the total amplitude M for the decay,

$M = \sum_n \rho_n e^{i\phi_n} A_n$, where n indicates the n th intermediate state and $\rho_n e^{i\phi_n}$ is the corresponding complex coefficient with magnitude ρ_n and phase ϕ_n . The model is symmetrized with respect to the two identical K_S^0 mesons. The two-body decay amplitude A_n is given by $A_n = P_n S_n F_n^r F_n^D$, where S_n is the spin factor [31], F_n^r and F_n^D are the Blatt-Weisskopf barrier factor of the intermediate state and the D_s^\pm meson [32], respectively, and P_n is the relativistic Breit-Wigner amplitude [33] describing the propagator of the intermediate resonance.

Contributions of intermediate resonances are determined by an unbinned maximum-likelihood fit to data. A combined probability density function (PDF) for the signal and background hypotheses is constructed, depending on the momenta of the three final-state particles. See Refs. [29,30,34] for details. The signal PDF is constructed from the total amplitude M . The background PDF, B , is constructed from a background shape derived from the inclusive MC samples using the kernel estimation method RooNDKeysPdf [35,36]. It models the distribution of an input dataset as a superposition of Gaussian kernels. This background PDF is then added to the signal PDF incoherently and the combined PDF is written as

$$\text{PDF} = \epsilon R_3 \left[\frac{f_s |M(p_j)|^2}{\int \epsilon |M(p_j)|^2 R_3 dp_j} + \frac{(1-f_s) B_\epsilon(p_j)}{\int \epsilon B_\epsilon(p_j) R_3 dp_j} \right],$$

where B_ϵ is defined as B/ϵ , ϵ is the acceptance in bins of the Dalitz plot determined with a MC sample of $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ uniformly distributed over the Dalitz plot. The placeholder $p_j = \{p_1, p_2, p_3\}$ represents the momenta of the final state particles, R_3 is the three-body phase-space element, and f_s is the purity. The normalization integral in the denominator is determined by a MC technique as described in Ref. [29,30].

The Dalitz plot of $M_{K_S^0 \pi^+}^2$ versus $M_{K_S^0 \pi^+}^2$ is shown in Fig. 1(a), symmetrized for the indistinguishable K_S^0 candidates (two entries per event). The strong vertical and

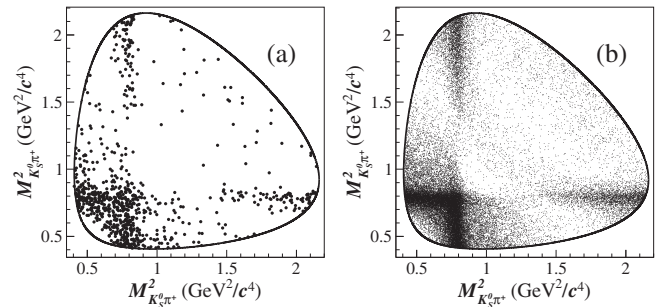


FIG. 1. Dalitz plot of $M_{K_S^0 \pi^+}^2$ versus $M_{K_S^0 \pi^+}^2$ for $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$, symmetrized for the indistinguishable K_S^0 candidates (two entries per event), of (a) the sum of all data samples and (b) the signal MC samples generated based on the amplitude analysis result. The black curve indicates the kinematic boundary.

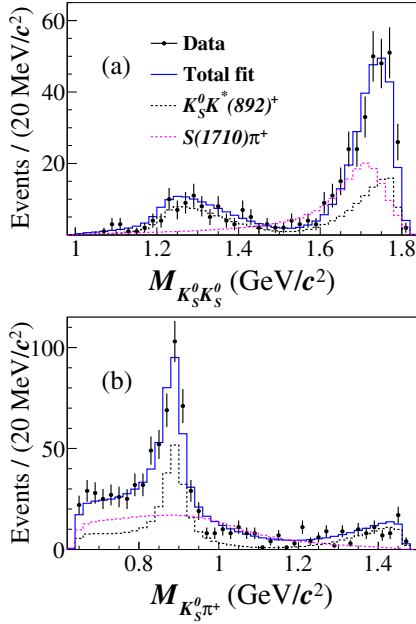


FIG. 2. Distribution of (a) $M_{K_S^0 K_S^0}$ and (b) $M_{K_S^0 \pi^+}$ from the nominal fit. The distribution of $M_{K_S^0 \pi^+}$ contains two entries per event, one for each K_S^0 . The data samples are represented by points with uncertainties and the fit results by the blue lines. Colored dashed lines show the individual components of the fit model. Due to interference effects, the total PDF is not necessarily equal to the sum of the components.

horizontal bands around $0.8 \text{ GeV}^2/c^4$ are caused by the process $D_s^+ \rightarrow K_S^0 K^*(892)^+$. We choose this process as a reference so that the magnitudes and phases of other amplitudes are to be understood as relative values with respect to this reference amplitude. The purity is a fixed quantity in the fit. Other possible contributions from resonances such as $K_1(1410)^+$, $K_0^*(1430)^+$, $S(980)$, $f_2(1270)$, $a_2(1320)$, $f_0(1370)$, $a_0(1450)$, $f_0(1500)$, $f_2(1525)$, $K^*(700)^+$, $K\pi$ LASS [37], K -matrix [38], $a_2(1700)$ and $S(1710)$ are added to the fit one at a time. The masses and widths of all resonances are fixed to the known values [4] apart from those of the $S(1710)$. The statistical significance of each new amplitude is calculated from the change of the log-likelihood taking the change in the number of degrees of freedom into account. Various combinations of these resonances are also tested. In addition to the reference amplitude $D_s^+ \rightarrow K_S^0 K^*(892)^+$, the amplitude for the decay $D_s^+ \rightarrow S(1710)\pi^+$ is found to have a significance larger than 10σ . No other contribution has a significance of more than 3σ . The significance of a $S(980)$ contribution is less than 1σ . The Dalitz plot of the signal MC sample generated based on the result of the amplitude analysis is shown in Fig. 1(b). The mass projections of the fit are shown in Fig. 2. The goodness of fit is $\chi^2/\text{NDOF} = 15.9/19 = 0.8$ and the p-value is 0.66 for Fig. 2(a) and $28.8/32 = 0.9$ and the p-value is 0.63 for Fig. 2(b), where NDOF is the number of degrees of freedom.

TABLE I. Fit fractions (FF) for the two amplitudes, and phase difference to the reference process. The first and the second uncertainties are statistical and systematic, respectively. The sum of the two FFs is 89.8%.

Amplitude	Phase	FF (%)
$D_s^+ \rightarrow K_S^0 K^*(892)^+$	0.0 (fixed)	$43.5 \pm 3.9 \pm 0.5$
$D_s^+ \rightarrow S(1710)\pi^+$	$2.3 \pm 0.1 \pm 0.1$	$46.3 \pm 4.0 \pm 1.2$

In the goodness of fit calculation, we merge neighboring bins until each bin has at least 10 entries. For the BFs of $S(980)$ decays, the magnitudes of the $S(980)$ decays is scanned to obtain the likelihood variation versus the expected BF and estimated systematic uncertainty. The likelihood is convolved with a Gaussian function with a width equal to the total systematic uncertainty.

The contribution of the n th amplitude relative to the total BF is quantified by the fit fraction (FF) defined as $\text{FF}_n = \int |\rho_n A_n|^2 dR_3 / \int |M|^2 dR_3$. The FFs for both amplitudes and the phase difference relative to the reference process are listed in Table I. The sum of the two FFs is 89.8%. The Breit-Wigner mass and width of the $S(1710)$ are determined to be $(1.723 \pm 0.011_{\text{stat}} \pm 0.002_{\text{syst}}) \text{ GeV}/c^2$ and $(0.140 \pm 0.014_{\text{stat}} \pm 0.004_{\text{syst}}) \text{ GeV}/c^2$, respectively.

Systematic uncertainties for the results of the amplitude analysis, including the phase difference, FFs, and the mass and the width of the $S(1710)$, are determined by differences between the results of the nominal fit and fits with the following variations. The mass and the width of the $K^*(892)^+$ are shifted by their uncertainties [4]. The radii of the Blatt-Weisskopf barrier factors are varied from their nominal values of 5 GeV^{-1} and 3 GeV^{-1} (for the D_s^+ meson and the intermediate resonances, respectively) by $\pm 1 \text{ GeV}^{-1}$. The uncertainties associated with the size of the background sample are studied by varying the purity within its statistical uncertainty. An alternative background sample is used to determine the background PDF, where the relative fractions of background processes from direct $q\bar{q}$ and non- $D_s^{*\pm} D_s^\mp$ open-charm processes are varied by the statistical uncertainties of the known cross sections. To estimate the systematic uncertainty related to the reconstruction efficiency, the amplitude analysis is performed varying the particle-identification and tracking efficiencies according to their uncertainties. The total uncertainties are obtained by adding these contributions in quadrature.

The BF of $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ is measured with the DT technique using the same tag modes and event selection criteria as in the amplitude analysis. However, the kinematic fit is not applied. We require the momentum of the isolated π^+ to be greater than $>0.1 \text{ GeV}/c$ to remove soft pions from D^{*+} decays. For each tag mode, the combination with recoiling mass closest to the known D_s^{*+} mass [4] is selected as the best ST candidate and the combination with the average mass of the tag D_s^- (M_{tag}) and the signal

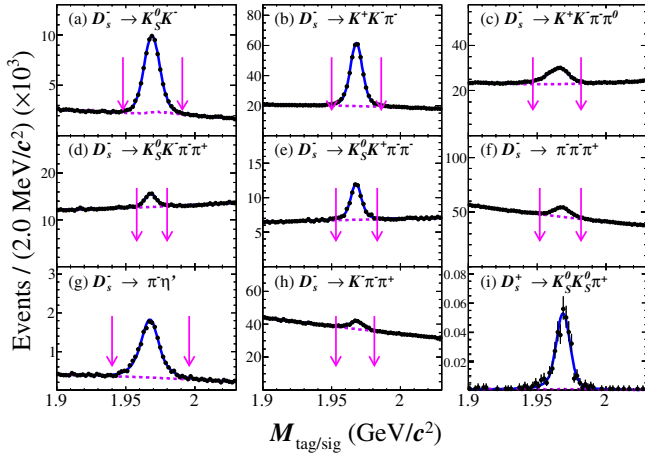


FIG. 3. Fits to (a)–(h) the M_{tag} distributions of the ST candidates and (i) the M_{sig} distribution of the DT signal candidates. The data samples are represented by points with uncertainties, the total fit results by solid blue lines and the background contributions by dashed violet lines. The pairs of pink arrows indicate the signal regions.

D_s^+ (M_{sig}) closest to the D_s^{*+} mass is selected as the best DT candidate. The BF is given by [29,30]

$$\mathcal{B}_{\text{sig}} = \frac{N_{\text{total, sig}}^{\text{DT}}}{\sum_{\alpha, i} N_{\alpha, i}^{\text{ST}} \epsilon_{\alpha, \text{sig}, i}^{\text{DT}} / \epsilon_{\alpha, i}^{\text{ST}}}, \quad (1)$$

where α runs over the various tag modes, and i denotes the different center-of-mass energies. The ST yields in data $N_{\alpha, i}^{\text{ST}}$ and the DT yield $N_{\text{total, sig}}^{\text{DT}}$ are determined by fits to the M_{tag} and M_{sig} distributions shown in Figs. 3(a)–3(f) and 3(i), respectively. The signal shape is modeled with the MC-simulated shape convolved with a Gaussian function. In the fits to the M_{tag} distributions, the background is parametrized as a second-order Chebyshev polynomial. For the tag modes $D_s^- \rightarrow K_S^0 K^-$ and $D_s^- \rightarrow \pi^- \eta'$, MC simulations of the decays $D^- \rightarrow K_S^0 \pi^-$ and $D_s^- \rightarrow \eta \pi^+ \pi^- \pi^-$ are added to the background to account for these peaking background contributions. In the fit to the M_{sig} distribution, the background is described by the background MC. The corresponding efficiencies ϵ are obtained by analyzing the inclusive MC samples, with the signal events for $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ generated based on the results of the amplitude analysis. The total ST yields of all tag modes and the DT yields are 531217 \pm 2235 and 371 \pm 21, respectively. The BF of $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ is determined to be (0.68 \pm 0.04_{stat} \pm 0.01_{syst})%.

We consider the following systematic uncertainties in the measurement of the BF. Varying the signal and background shapes and taking into account the background fluctuation, the uncertainty on the total number of ST D_s^- candidates is 0.4%.

The uncertainty associated with the background shape in the fit to the DT M_{sig} distribution is 0.3%, determined by

replacing the nominal background shape with a second-order Chebyshev function and taking the difference between the two results. The uncertainty of the K_S^0 reconstruction efficiency is examined using control samples of $J/\psi \rightarrow K_S^0 K^\pm \pi^\mp$ and $\phi K_S^0 K^\pm \pi^\mp$ decays, and the data-MC efficiency ratio is (101.01 \pm 0.53)% [39]. We correct the signal efficiencies by this factor, and use the uncertainty of 0.53% as a systematic uncertainty. The π^+ tracking efficiencies are studied with $e^+ e^- \rightarrow K^+ K^- \pi^+ \pi^-$ events. The data-MC efficiency differences of the π^+ particle-identification and tracking are both 1.0%. The uncertainty from the signal MC based on the results of the amplitude analysis is studied by varying the fit parameters according to the covariance matrix. The change of signal efficiency is estimated to be 0.5%. The uncertainty due to the limited MC sample size is obtained from $\sqrt{\sum_{\alpha, i} (f_{\alpha, i} \frac{\delta_{\epsilon_{\alpha, i}}}{\epsilon_{\alpha, i}})^2}$, where $f_{\alpha, i}$ is the tag yield fraction, and ϵ_i and δ_{ϵ_i} are the signal efficiency and the corresponding uncertainty of tag mode α and center-of-mass energy i , respectively. It is found to be 0.2%. In total, the systematic uncertainty on the branching fraction is 1.9%.

In summary, we present the first amplitude analysis of the decay $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ using 6.32 fb $^{-1}$ of $e^+ e^-$ annihilation data taken at center-of-mass energies between 4.178 and 4.226 GeV. The results are listed in Table I. The Breit-Wigner mass and width of the $S(1710)$ are measured to be (1.723 \pm 0.011_{stat} \pm 0.002_{syst}) GeV/ c^2 and (0.140 \pm 0.014_{stat} \pm 0.004_{syst}) GeV/ c^2 , respectively. These parameters are consistent with the PDG evaluation for the $f_0(1710)$ within 1.2 σ and 0.7 σ , respectively [4].

The BF of $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ is determined to be (0.68 \pm 0.04_{stat} \pm 0.01_{syst})%, which is consistent with the CLEO result $\mathcal{B}(D_s^+ \rightarrow K_S^0 K_S^0 \pi^+) = (0.77 \pm 0.05_{\text{stat}} \pm 0.03_{\text{syst}})\%$ [4,17] within 1.3 σ . The BFs for the two intermediate processes are calculated with $\mathcal{B}_i = \text{FF}_i \times \mathcal{B}(D_s^+ \rightarrow K_S^0 K_S^0 \pi^+)$, as shown in Table II. The BF of $D_s^+ \rightarrow K_S^0 K^*(892)^+ \rightarrow K_S^0 K_S^0 \pi^+$ is determined to be (3.0 \pm 0.3_{stat} \pm 0.1_{syst}) $\times 10^{-3}$. This leads to $\mathcal{B}(D_s^+ \rightarrow \overline{K^0} K^*(892)^+) = (1.8 \pm 0.2_{\text{stat}} \pm 0.1_{\text{syst}})\%$ which deviates from the CLEO result of this BF, (5.4 \pm 1.2)% [4,40], by 2.9 σ . However, Ref. [40] does not consider interference terms.

Because a significant $D_s^+ \rightarrow S(980) \pi^+$ contribution is observed in the amplitude analysis of $D_s^+ \rightarrow K^+ K^- \pi^+$

TABLE II. BFs for amplitudes with the final state $K_S^0 K_S^0 \pi^+$. The first and the second uncertainties are statistical and systematic, respectively.

Amplitude	BF (10^{-3})
$D_s^+ \rightarrow K_S^0 K^*(892)^+ \rightarrow K_S^0 K_S^0 \pi^+$	3.0 \pm 0.3 \pm 0.1
$D_s^+ \rightarrow S(1710) \pi^+ \rightarrow K_S^0 K_S^0 \pi^+$	3.1 \pm 0.3 \pm 0.1

[13], one would expect that about 10% of the signal comes from $D_s^+ \rightarrow S(980)\pi^+$ with $S(980) \rightarrow K_S^0 K_S^0$ [4]. However, almost no signal populates the region below $1.1 \text{ GeV}/c^2$ in the $K_S^0 K_S^0$ mass spectrum. The upper limit of $\mathcal{B}(D_s^+ \rightarrow S(980)\pi^+)$ is determined to be 1.8×10^{-4} at the 90% confidence level. This suppression can likely be attributed to destructive interference between $a_0(980)^0$ and $f_0(980)$ in decays to two neutral kaons. The same interference term would then be constructive in decays to two charged kaons, explaining the large branching fraction observed there. On the other hand, an enhancement is seen in the $K_S^0 K_S^0$ mass spectrum around $1.7 \text{ GeV}/c^2$. Reference [13] reports $\mathcal{B}(D_s^+ \rightarrow f_0(1710)\pi^+, f_0(1710) \rightarrow K^+ K^-) = (0.10 \pm 0.02_{\text{stat}} \pm 0.03_{\text{syst}})\%$. This corresponds to an expected BF of about 5×10^{-4} for $D_s^+ \rightarrow f_0(1710)\pi^+, f_0(1710) \rightarrow K_S^0 K_S^0$, based on isospin symmetry predicting the ratio $\frac{\mathcal{B}(f_0(1710) \rightarrow K^+ K^-)}{\mathcal{B}(f_0(1710) \rightarrow K_S^0 K_S^0)}$ to be two. In our amplitude analysis, we determine this BF to be $(3.1 \pm 0.3_{\text{stat}} \pm 0.1_{\text{syst}}) \times 10^{-3}$, which is one order of magnitude larger than the expectation. Based on the same argument concerning the difference in interference between pairs of charged and neutral kaons in isospin one and isospin zero configurations, this observation implies the existence of an isospin one partner of the $f_0(1710)$ meson, the $a_0(1710)^0$, as proposed by Refs. [1,2] and as recently observed in Ref. [7]. The $f_0(1710)$ and $a_0(1710)^0$ amplitudes could then interfere constructively in decays to two neutral kaons and destructively in decays to two charged kaons, explaining the different observations made in this work and in Ref. [13]. Taken together, these results are more consistent with the $K^* \bar{K}^*$ molecule hypothesis of $f_0(1710)$. A simultaneous amplitude analysis of $D_s^+ \rightarrow K^+ K^- \pi^+$ and $D_s^+ \rightarrow K_S^0 K_S^0 \pi^+$ can further clarify this situation. In addition, a charged partner of $a_0(1710)^0$ is expected to be visible in the $K_S^0 K^+$ mass spectrum in the related decay $D_s^+ \rightarrow K_S^0 K^+ \pi^0$ [41].

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